

1 **Space-Efficient, Side-Channel Attack Resistant Table Lookups**

2 **PRIORITY**

3 This application claims priority to Provisional application entitled, "A Technique for  
4 Space-Efficient, Side-Channel Attack Resistant Table Lookups ", attorney [agent] docket  
5 number, YOR920010711US1, filed, August 14, 2001, assigned serial number, 60/312204.

6 **CROSS REFERENCE**

7 This application is cross-referenced to US patent application, entitled, "METHOD AND  
8 DEVICE FOR SECURELY HANDLING INFORMATION IN A CRYPTOGRAPHIC  
9 INFORMATION PROCESSING SYSTEM," Docket Number GE998-073, assigned Serial  
10 Number 09/240,503, filed January, 29, 1999, which is incorporated herein by reference in  
11 entirety for all purposes.

12 **FIELD OF INVENTION**

13 This invention relates to the field of information security. More particularly, it relates to  
14 processing of sensitive data.

15 **BACKGROUND OF THE INVENTION**

16 The field of information security deals with methods and mechanisms to protect sensitive  
17 information. Some of these methods and mechanisms deal with the problem of maintaining the  
18 integrity of information while it is in storage or in transit, others deals with the issue of ensuring  
19 that the information is available only to authorized entities and access is denied to entities not so

1 authorized. Several of the methods and mechanisms used in the field of information security are  
2 based on the use of Cryptographic Algorithms. Table lookup is a fundamental primitive used by  
3 many cryptographic algorithms such as the Data Encryption Standard (DES), Advanced  
4 Encryption Standard (AES) , the popular A3/A8 algorithm used in GSM cell-phones which is  
5 known as COMP128 etc. Table lookups are also used by some non-cryptographic algorithms in  
6 the field of information security. For example, universal hash functions are traditionally not  
7 considered to be cryptographic algorithms although they are used for ensuring the integrity of  
8 information and some universal hash functions are based on table lookups. Thus, Table lookup  
9 is an important primitive used in the field of information security.

10 In its simplest form, a Table is a collection of data values wherein each of said data values in said  
11 collection has a distinct index. The Table lookup operation then comprises of obtaining the data  
12 value that corresponds to a supplied index. The total amount of memory needed to store a Table,  
13 that is, to store the entire collection of data values is referred to as the lookup table size. In  
14 addition, the total number of distinct indices in the collection, which by definition is the number  
15 of data values in the collection, is referred to as the table lookup index size. For any given table  
16 T, hereinafter, we shall use the notation  $T[i]$  to refer to the data value that corresponds to the  
17 index i. Thus although the present application is described in terms of tables and table lookup  
18 operations it includes all means of representing collections of data such as arrays, matrices,  
19 ordered sets, lists, groups, collections etc.

20 Implementing the Table lookup primitive in situations where information security is not an issue  
21 is usually straightforward. In fact , Table lookup is such a basic primitive that many general  
22 purpose computing platforms have specialized hardware to assist in this operation, for example  
23 many microprocessors have an indexed addressing mode where one supplies the location of a  
24 table in the memory of a computing system and an index into the table and the hardware retrieves  
25 the data value corresponding to the index.

26 However, in situations where information security is an issue, implementing a Table lookup is  
27 substantially harder. This is because this operation has to be performed on some information

1 processing equipment which is a physical system. The Table lookup operation that has to be  
2 performed could involve information which is sensitive in nature and disclosure of this  
3 information or part thereof to unauthorized entities must be prevented. For example, the index  
4 being accessed in the Table lookup operation and/or the data value corresponding to the index  
5 could be sensitive. All physical information processing systems leak information about their  
6 internal states into the physical environment in which they are placed. Such leakage occurs in a  
7 variety of ways. For example, the instantaneous power consumption of a system conveys  
8 information about the operations being carried out by the device at that time, the timing of  
9 certain operations conveys information about the operations, the electromagnetic emissions from  
10 a device carry information about the operations being done on the device, etc. In the field of  
11 information security it is customary to call these additional sources of information as  
12 Side-Channels. It is well known that information security can be seriously compromised if  
13 Side-Channel information is available to unauthorized entities. In fact, there is a large class of  
14 attacks, known in the literature, in which an unauthorized entity gets sensitive information by  
15 exploiting side-channel information, some examples being Timing attacks (TA), Simple Power  
16 Analysis attacks (SPA), Differential Power Analysis attacks (DPA), Simple Electromagnetic  
17 Analysis attacks (SEMA), Differential Electromagnetic Analysis attacks (DEMA), higher-order  
18 DPA, higher-order DEMA etc. Hereinafter we will use the generic term side-channel attacks to  
19 include all attacks which involve analysis of any side-channel. This term includes TA, SPA,  
20 DPA SEMA, DEMA etc. We use the generic term, higher-order side-channel attacks, to include  
21 all attacks which involve the analysis of multiple side-channels or multiple sections the same  
22 side-channel or both. This generic term includes higher-order DPA, higher-order DEMA etc.  
23 Therefore, if a Table lookup involving sensitive information is to be performed within a physical  
24 system then special care must be taken to limit the information leakage from various  
25 Side-Channels in the scenario where an unauthorized entity can have access to these  
26 Side-Channels. This makes the implementation of a Table lookup much more complex in this  
27 scenario. In addition, implementing Table lookup on resource constrained information  
28 processing devices such as chip cards, cryptographic tokens etc., poses a special challenge since  
29 these devices are less shielded from the environment and therefore have larger leakage of  
30 information via various side-channels. In general, it is reasonable to assume that in performing a

1 table lookup the information obtained via the side channel is statistically related to each bit of the  
2 index being addressed and to each bit of the data value corresponding to the index.

3  
4 Many mechanisms and countermeasures are known in prior art, have been proposed to reduce the  
5 effectiveness of side-channel exposures in constrained information processing devices. These fall  
6 into two main categories. In the first category are physical protection methods which try to  
7 reduce the amount of information leakage from the device itself, e.g., the use of physical  
8 shielding and techniques for hardware design which minimize the leakage of information. Use of  
9 these techniques result in devices which inherently leak less information on the side-channels  
10 than devices which are not thus protected. However, the leakage is not entirely eliminated. In  
11 most situations, even after the application of these physical protections, there is enough  
12 information leakage so that implementations of information security techniques on such devices  
13 can be attacked using statistical side-channel attacks such as DPA, DEMA, higher-order DPA,  
14 higher-order DEMA etc. To overcome this problem, there is another category of protection  
15 mechanisms which are based on reducing the effectiveness of the information that does leak on  
16 the side-channels. These type of protections require a careful implementation of information  
17 security techniques on the device, where the implementation is quite different from the obvious  
18 and direct implementations of the technique. Most of these latter protection mechanisms are  
19 either based on or similar to a generic method and technique outlined in, "Towards Sound  
20 Approaches to Counteract Power Analysis Attacks," authored by Suresh Chari, Charanjit S.  
21 Jutla, Josyula R. Rao and Pankaj Rohatgi, which appears in proceedings of "Advances in  
22 Cryptology- CRYPTO '99", Lecture Notes in Computer Science, # 1666, published by Springer,  
23 Pages 398-412, which is incorporated herein by reference in entirety for all purposes. The  
24 present invention can be viewed as a substantial improvement to the table lookup scheme  
25 suggested in that publication. Since the present invention of a space-efficient, side-channel  
26 attack resistant table lookup mechanism would be part of a larger side-channel attack resistant  
27 implementation of any information security technique which involves table lookups as well as  
28 other operations, we now describe the generic method and technique, hereinafter referred to as  
29 the "General Countermeasure Against Side-channel Attacks" which is disclosed in the

1 aforementioned publication. The next few paragraph is an adaptation from the original paper  
2 which described the technique and is therefore put in quotes.

3 **“A General Countermeasure**

4 A General Countermeasure Against Side-Channel Attacks is to ensure that the adversary cannot  
5 predict any relevant bit of information from the side-channel in any clock cycle, without making  
6 run--specific assumptions independent of the actual inputs to a computation. This makes  
7 statistical tests involving several experiments impossible, since the chance of the adversary  
8 making the correct assumptions for each run is extremely low. While this yields secure  
9 computation, it is not clear how one can do effective computation under this requirement since  
10 no bit depending directly on the data and key can be manipulated at any cycle. In some cases the  
11 function being computed has algebraic properties that permits such an approach, e.g., for RSA  
12 one could use the well known blinding technique to partially hide the actual values being  
13 manipulated. Another class of problems where this is possible is the class of random  
14 self-reducible problems. Such structure is unlikely to be present in primitives such as block  
15 ciphers.”

16 **“Encoding**

17 The encoding we propose is to randomly split every bit of the original computation, into  $k$  shares  
18 where each share is equiprobably distributed and every proper subset of  $(k-1)$  shares is  
19 statistically independent of the encoded bit. Computation can then be carried securely by  
20 performing computation only the shares, without ever reconstructing the original bit. Shares are  
21 refreshed after every operation involving them to prevent information leakage to the adversary.”

22 “To fix a concrete encoding scheme, we assume that each {\em bit} is split into  $k$  shares using  
23 any scheme which has the required stochastic properties. For instance, bit  $b$  can be encoded as  
24 the  $k$  shares  $b \oplus r_1, r_2, \dots, r_{k-1}, r_1 \oplus \dots \oplus r_{k-1}$ , where the  $r_i$  ‘s are randomly chosen bits.  
25 Furthermore, assume that each share is placed in a separate word at a particular bit position and  
26 all other bits of the share word are chosen uniformly at random.”

1 “In practice, it would be more useful, if each word of computation is split similarly into k shares.  
2 In that case, other schemes of splitting into shares based on addition mod 256, subtraction mod  
3 256 would also be viable. Encoding bytes of data manipulated by splitting them into shares  
4 would yield the optimal performance. Ignoring the initial setup time, the performance penalty in  
5 performing computation using just the k shares is a factor of k. Our results which have been  
6 proved based on the bit encoding scheme would also work for this case but the bounds they yield  
7 are based only on the characteristics of the noise within the chip, and hence may not be optimal.  
8 This is discussed briefly after the analysis for the bit encoding case. The results and analysis we  
9 present here can serve as a framework in which to prove results for the byte  
10 encoding scheme.”

11 “The method to encode the bit in secret shares should be chosen based on the computation being  
12 protected. For instance, for an implementation of DES, the XOR scheme is ideal since the basic  
13 operations used are XOR, permutations, and table lookups. Table lookups can be handled by  
14 first generating a random rearrangement of the original table since a randomized index will be  
15 used to look up the table. This step increases the overhead beyond the factor of 2.”

16 “In practice, the splitting technique needs to be applied only for a sufficient number of steps into  
17 the computation until the adversary has very low probability of predicting bits, i.e., till sufficient  
18 secret key dependent operations have been carried out. Similar splitting also has to be done at  
19 end of the computation if the adversary can get access to its output. For instance, in DES, one  
20 needs to use the splitting scheme only for the first four and last four rounds.”

21 Thus, the above publication provides a general countermeasure against side-channel attacks,  
22 which is to split each bit or word of the computation into k shares (where k is any integer such as  
23 2, 3, 4,..., etc.) with specific statistical properties. Hereinafter we will refer to any such  
24 mechanism to split any bit or word in a computation to be a “secret-sharing operation”. Thus the  
25 countermeasure for any information security techniques will work by splitting all inputs into  
26 shares using a secret-sharing operation, performing computation on the shares to obtain shares of  
27 the output and then recombining the shares of the output using the inverse of secret-sharing

1 operation to produce the output. However, the mechanism proposed to deal with Table lookups,  
2 which is to create a random rearrangement of the original table (which has to be in RAM ) is  
3 inefficient, since the random rearrangement of a table in RAM will take as much space as the  
4 size of the table. Thus in prior art, reducing the exposures from side-channels during table  
5 lookups has been the most challenging since many good countermeasures require much more  
6 Read/Write memory (such as RAM) than these devices can spare. Further, the limited addressing  
7 capabilities of such devices often complicates lookups of large tables, sometimes leading to new  
8 side-channel exposures. For example, many smart cards have a total of only 256-512 bytes of  
9 RAM. A significant part of this memory is required for the regular functioning of these smart  
10 cards and therefore only a fraction of this total RAM can be made available for countermeasures  
11 against side channel leakage. In many scenarios, the amount of RAM available for  
12 countermeasures, which is hereinafter referred to as available RAM is significantly less than the  
13 lookup table size. For example the COMP 128 algorithm requires lookup of a table of size 512  
14 bytes and index size of 512 and several other smaller tables, and the DES algorithm requires the  
15 lookup of eight tables of size 64 bytes and index size 64 each for a total of 256 bytes. Many  
16 chip cards have no more than 256 bytes of RAM and the available RAM is even smaller and this  
17 means that good known countermeasures cannot be applied to such cards to protect against side  
18 channel attacks for algorithms such as DES, COMP128 etc. In addition many smart cards are  
19 8-bit machines and can lookup indices only within the range 0 to 255 , within a table of bytes at  
20 any one time. This leads to problems if the smart card is required to access a table of bytes with  
21 larger index size than 256. For example, the COMP128 table with 512 byte table size and index  
22 size of 512 cannot be looked up in a single operation on such a chip card and any such operation  
23 has to be implemented as a sequence of operations. Having a sequence of operations to  
24 implement a Table lookup opens up additional avenues for attack using side-channels.

25 As a result of these limitations, heretofore side-channel attack resistant implementations many  
26 algorithms which utilized the Table lookup operation required the use of more expensive devices  
27 which had more RAM, or these implementations were either unacceptably slow or are still  
28 susceptible to side channel attacks.

1 The terms set and subset as used herein is used as in mathematics. Thus, a set refers to a  
2 collection of elements. A subset of a set refers to another collection of zero or more elements  
3 from said set including the total set.

4 **SUMMARY OF THE INVENTION**

5 In a first aspect this patent provides methods and apparatus to create efficient side channel attack  
6 resistant implementation of table lookups. This generally results in use of less RAM than the  
7 size of the table being accessed. In addition, in many embodiments of the present invention, the  
8 invention solves problems related to information leakage when accessing tables having large  
9 indices.

10 An additional aspect of the presentation is provision of a substantial improvement of other  
11 approaches which provided resistance against side-channel attacks using as much RAM as the  
12 size of the table being accessed by exploiting tradeoffs between RAM usage and additional  
13 accesses to ROM. This tradeoff is advantageous in applications where the cost of requiring extra  
14 access to ROM is significantly less than the cost of including additional RAM resources into the  
15 device.

16 Another aspect of the invention is that the RAM usage and ROM access tradeoff is achievable  
17 in a manner that preserves the resistance of the implementation to side channel vulnerabilities.

18 **BRIEF DESCRIPTION OF THE DRAWINGS**

19 These and other aspects, features, and advantages of the present invention will become apparent  
20 upon further consideration of the following detailed description of the invention when read in  
21 conjunction with the drawing figures, in which:

1 Fig. 1, shows an example of a flow chart of a process by which N byte table T is split into the  
2 two tables U1 and U2 of size  $N/2$  bytes each using the Two-way Byte Table Splitting Method;

3 Fig. 2, shows an example of a process to lookup  $T[i]$  when T has been split into tables U1 and  
4 U2 using the Two-way Byte Table Splitting Method;

5 Fig. 3, shows an example of a flow chart of a process to split a N byte table T into m tables U1,  
6 U2... Um of size  $N/m$  bytes each using the Output Divisor Table Splitting Method;

7 Fig. 4, shows an example of a process to lookup  $T[i]$  when T has been split into m tables U1, U2,  
8 ...., Um using the Output Divisor Table Splitting Method;

9 Fig. 5, shows an example of a flow chart for the Table Mask operation using the Input-Output  
10 Permutation Masking Method;

11 Fig. 6, shows an example of a process to lookup  $T[i]$  when table T has been masked using the  
12 Input-Output Permutation Masking Method.

13 Fig. 7, shows an example of a flow chart for the Table Mask operation using the Input-Output  
14 XOR Permutation Masking Method;

15 Fig. 8, shows an example of a process to lookup  $T[i]$  when table T has been masked with using  
16 the Input-Output XOR Permutation Masking Method;

17 Fig. 9, shows an example of a process which combines data values from m tables V1,..,Vm  
18 having same index size N to form a single table W having an index size of N using the  
19 Entry-wise Algebraic Aggregate method based on the algebraic operator “opn”;

1 Fig. 10, shows an example of a process which recovers the data value  $V1[i]$  from the table W and  
2 tables  $V2,..,Vm$ , where W was created as shown in Figure 9 from  $V1,..,Vm$  using the  
3 Entry-wise Algebraic Aggregate method;

4 Fig. 11, shows an example of a process which combines data values from 2 tables  $V1,V2$  having  
5 same index size N to form a single table W having an index size of N using the Byte-wise XOR  
6 Aggregate Method;

7 Fig. 12, shows an example of a process which recovers the data value  $V1[i]$  from the table W and  
8 table  $V2$  in created in Fig. 11 using the Byte-wise XOR Aggregate Method;

9 Fig. 13, shows an example of a summary of a process to set up the infrastructure to perform table  
10 lookups of one or more known lookup tables, each of these known lookup tables having a  
11 particular table size and a particular table index size, in a side-channel attack resistant manner  
12 with the constraints of M bytes of available RAM and a limit on addressing capability;

13 Fig 14, shows an example of a process of looking up the data value  $T[i]$  in a known table T,  
14 when T has been first split into table U1 and U2 using the Two-way Byte Table Splitting  
15 Method, U1 and U2 have been masked to produce tables  $U1'$  and  $U2'$  using the Input-Output  
16 XOR Permutation Masking method and masked with  $r1,r2$  and  $s1,s2$  respectively, and  $U1'$  and  
17  $U2'$  then aggregated into a an aggregate table W using the Byte-wise XOR Aggregate Method.  
18 W is in RAM and U1,U2 are in ROM; and

19 Fig 15, shows an example of a generic diagram of an apparatus realizing present invention;

20 **DESCRIPTION OF THE INVENTION**

21 This patent provides ways to create an efficient side channel attack resistant implementation of  
22 table lookups using much less RAM than the size of the table being accessed. In addition, in

1 many cases this solution also takes care of the problem of dealing with tables having index size  
2 which is too large to be lookup up in a single operation..

3 One of the problems being solved by this invention is the following: An information processing  
4 operation needs to be performed involving lookups of at least one known lookup table. Each  
5 particular table from said at least one known lookup table having a particular lookup table size  
6 and a particular lookup table index size. There is a certain amount of available RAM for this  
7 operation and the operation needs to be implemented efficiently within the available amount of  
8 RAM in a manner which resists side-channel attacks. In mathematical notation, therefore we  
9 have  $p$  known lookup tables  $T_1, T_2, T_3, \dots, T_p$  for some integer  $p > 0$  and we have  $M$  bytes of  
10 available RAM.

11 The invention is best taught in terms of the application of three building blocks, the Table Split  
12 operation, the Table Mask operation and the Table Aggregate operation which are described  
13 herein.

14 **The "Table Split" operation:**

15 This operation is used for a known table  $T$  if there is too little RAM to hold the entire table  $T$  or  
16 the index requirements of  $T$  are more than the addressing abilities of the device implementing the  
17 table lookup. That is, the particular table  $T$  has particular lookup table size more than  $M$  bytes or  
18 the particular table  $T$  has particular lookup table index size which exceeds the maximum index  
19 the device can use to address a table in memory.

20 Let  $n$  be the number of bits required to represent any possible index of the lookup table  $T$ . Let  $b$   
21 be the number of bits required to represent any possible data value in the lookup table  $T$ .  
22 Hereinafter we will refer to any such  $T$  as a  $n$ -bit to  $b$ -bit table.

23  
24 The  $n$ -bit to  $b$ -bit table  $T$  is to be then split into a collection of  $k$  split tables  $U_1, U_2, \dots, U_k$  such  
25 that each split table has smaller table size and/or smaller table index size than  $T$ . Furthermore,

1 any lookup into the table T and be accomplished by a sequence of lookups into these split tables  
2 U1,...,Uk. Table splitting can be accomplished in a variety of ways as known to those skilled in  
3 the art becoming familiar with the spirit and concepts presented herein.

4 For the purposes of exposition, first a simple method herein referred to as "**Two-way Byte**  
5 **Table Splitting Method**", is described which splits a n-bit to 8-bit table T into two (n-1)bit to 8  
6 bit tables U1 and U2 and it is shown how U1 and U2 can be used in place of T, for the purpose of  
7 table lookup. Subsequently a more general method is herein referred to as the "**Output Divisor**  
8 **Table Splitting Method**" is described which splits a n-bit to b-bit table T into m equal sized  
9 tables U1,...Um where m is any divisor of b and it is shown how U1,..,Um can be used in place  
10 of T. The methods described herein result in split tables all having equal size. This is because in  
11 many applications it is advantageous to have split tables be of equal size. We will also describe  
12 at a higher level how the table could be split unequally. Therefore, even though the detailed  
13 descriptions provided herein produce split tables of equal size, those with ordinary skill in the art  
14 can easily apply the methods described herein and obvious variants thereof to create tables  
15 which are of unequal size and in that sense this invention also covers the case where the split  
16 tables are of unequal size.

17 First, a simple splitting scheme is described for a Two-way Byte Table Splitting Method, that  
18 splits a n-bit by 8-bit table T of table size N bytes into two (n-1)-bit by 8-bit tables U1 and U2 of  
19 size N/2 bytes each and uses U1 and U2 instead of T for the purposes of table lookup.

20 Essentially U1 contains the compacted form of the first nibbles of the data values of T and U2  
21 contains the compacted form of the second nibbles of T. The full details of one method of  
22 performing this split is illustrated in Figure 1 which provides a flow chart of a process which  
23 splits T into the two tables U1 and U2. Since the table T is of size N bytes and the data values  
24 are each of size 1 byte, without loss of generality, assume the index runs from 0 through N-1.  
25 The process starts (100) by setting a loop variable "i" to the value of 0. A process of splitting the  
26 data value of T having the i'th index is then performed in a loop for each value of "i" from 0 to  
27 N-1. The loop for the variable "i" is realized using a comparison step (101) and an increment step  
28 (107). In the comparison step, it is verified that the value of "i" is less than N and if not the

1 process is terminated (102) or else the processing continues on with step (103). The increment  
2 step (107) increments the value of “i” by 1 and then jumps to the comparison step. For each  
3 valid value of “i”, the following is performed. First, variables “j”, “k”, “L” and “U” are set based  
4 on the current value of “i” and T[i] (103). The variable “j” is set to “(i div 2)” which is the  
5 largest integer less than or equal to (i/2). The variable “k” is set to “(i mod 2)”, the parity of “i”.  
6 The variable “L” is set to the first nibble (least significant 4-bits) of the byte T[i]. The variable  
7 “U” is set to the second nibble (most significant 4-bits) of the byte T[i]. Then in step (104) the  
8 parity variable “k” is compared to 0. If “k” equals 0, then step (105) is performed else step (106)  
9 is performed. In step (105) the first nibbles of the j’th data value of U1 and U2 are set to the  
10 values “L” and “U” respectively that were computed in step (103) and then step (107) is  
11 performed. In step (106), the second nibbles of the j’th data value of U1 and U2 are set to the  
12 values “L” and “U” respectively that were computed in step (103) and then step (107) is  
13 performed.

14 This completes a detailed description of implementation employing a Two-way Byte Table  
15 Splitting Method in which U1 and U2 are derived from T. In order to use these split tables in  
16 place of T, the process of obtaining T[i] from U1 and U2 is now described. Briefly, since U1  
17 contains the compacted form of the first nibbles of data values of T and U2 contains the second  
18 nibbles, the lookup of the value T[i] is done using U1 and U2 by locating the first nibble of T[i]  
19 in U1 and the second nibble of T[i] in U2 and combining these two nibbles. Figure 2 provides  
20 detailed flowchart of a process to lookup T[i] when T has been split into tables U1 and U2 using  
21 the Two-way Byte Table Splitting Method. As a first step (200) variables “j” and “k” are set  
22 based on the value of i. The variable “j” is set to be the largest integer less than or equal to i/2  
23 and “k” is set to be (i mod 2), that is the parity of i. Then a decision is made depending on the  
24 value of the parity (201). If the parity is even, that is “k” equals 0, then step (202) is performed  
25 else step (203) is performed. In step (202) the variable “a” is set to be the first nibble of U1[j]  
26 and the variable “b” is set to be the first nibble of U2[j]. Then a byte sized variable called  
27 “result” is computed by setting the first nibble of “result” as “a” and the second nibble of “result”  
28 as “b”. By the way the tables U1 and U2 are created, the value of “result” will be the same as the  
29 value T[i] and thus the value of T[i] can be assumed to be equal to that of “result” (204). In case

1 step (203) is performed ( instead of (202) ), then the variable “a” is set to be the second nibble of  
2 U1[j] and the variable “b” is set to be the second nibble of U2[j]. Then a byte sized variable  
3 called “result” is computed by setting the first nibble of “result” as “a” and the second nibble of  
4 “result” as “b”. By the way the tables U1 and U2 are created, the value of “result” will be the  
5 same as the value T[i] and thus the value of T[i] can be assumed to be equal to that of “result”  
6 (204).

7 This completes the detailed description of the Two-way Byte Table Splitting Method which splits  
8 a n-bit by 8-bit table T of table size N bytes into two (n-1)-bit by 8-bit tables U1 and U2 of size  
9 N/2 bytes each and uses U1 and U2 instead of T for the purposes of table lookup. Next a more  
10 general scheme herein referred to as the “ **Output Divisor Table Splitting Method** ” is  
11 described which splits a n-bit to b-bit table T into m equal sized tables U1,...Um where m is any  
12 divisor of b and it is shown how U1,..,Um are used in place of T. Essentially each Ui contains, in  
13 compacted form, the bits  $((b/m)*i)$  through  $((b/m)*(i+1)-1)$  of the data values of T. In this  
14 respect, the Two-way Byte Splitting Method scheme can be viewed as a special case of this  
15 scheme with m=2 and b=8. The full details of one method of performing this split is illustrated in  
16 Figure 3 which provides a flow chart of a process which splits the N byte table T into m tables  
17 U1, U2 ... Um of size  $N/m$  bytes each using the Output Divisor Table Splitting Method. Since the  
18 table T is of size N bytes and the data values are each of size 1 byte, without loss of generality,  
19 assume the index runs from 0 through N-1. The process starts (300) by setting a loop variable “i”  
20 to the value of 0. A process of splitting the data value of T having the i'th index is then  
21 performed in a loop for each value of “i” from 0 to N-1. The loop for the variable “i” is realized  
22 using a comparison step (301) and an increment step (307). In the comparison step, it is verified  
23 that the value of “i” is less than N and if not the process is terminated (302) or else the  
24 processing continues on with step (303). The increment step (307 ) increments the value of “i” by  
25 1 and then jumps to the comparison step. For each valid value of “i”, the following is performed.  
26 First variables “j”, “k”, “B1” ,.., “Bm” are set based on the current value of “i” and the value of  
27 T[i] (303). The variable “j” is set to  $(i \text{ div } m)$  which is the largest integer less than or equal to  
28  $(i/m)$ . The variable “k” is set to  $(i \text{ mod } m)$ . The variables “B1”,.., “Bm” are set as follows: “B1”  
29 is set to be the first set of  $(b/m)$  bits of T[i]; “B2” is set to the second set of  $(b/m)$  bits of T[i] (the

1 next least significant (b/m) bits) and so on and finally “Bm” is set to be the last (b/m) bits of T[i]  
2 (the most significant (b/m) bits). Then in step (311) the variable “k” is compared to 0. If “k”  
3 equals 0, then step (321) is performed else in step (312) the variable “k” is compared to 1 and if  
4 equal then step (322) is performed and so on till one by one all possible values of “k” which  
5 range from 0 to m-1 are exhausted. Finally if “k” happens to be “m-1”, this check is performed in  
6 step (31m) and step (32m) is performed. Thus one of steps (321),(322) ...., (32m) is performed  
7 based on the value of “k”. In step (321) the first (b/m) bits of U1[j], ..., Um[j] are set to the  
8 values “B1”,..., “Bm” respectively, which were computed earlier in step (303). In step (322) the  
9 second (b/m) bits of U1[j], ..., Um[j] are set to the values “B1”,..., “Bm” respectively, which  
10 were computed earlier in step (303) and so on, and in step (32m) the last (b/m) bits of U1[j], ...,  
11 Um[j] are set to the values “B1”,..., “Bm” respectively, which were computed earlier in step  
12 (303). Any one of steps (321),(322) ...., (32m) is followed by step (307).

13 This completes a detailed description of how U1, U2, ..., Um are derived from T using the  
14 Output Divisor Table Splitting Method. In order to use these split tables in place of T, the  
15 process of obtaining T[i] from U1,...,Um is now described. Briefly, since U1 contains the  
16 compacted form of the first (b/m) bits of data values of T and U2 contains the second (b/m) bits  
17 and so on and Um contains the last (b/m) bits, the lookup of the value T[i] is done using  
18 U1,...,U,m by locating the first (b/m) bits of T[i] in U1 and the (b/m) bits of T[i] in U2 and so on  
19 and the last (b/m) bits in Um and combining these bits. Figure 4 provides detailed flowchart of a  
20 process to lookup T[i] when T has been split into tables U1,...,Um according to the Output  
21 Divisor Table Splitting Method. As a first step (400) variables “j” and “k” are set based on the  
22 value of i. The variable “j” is set to be the largest integer less than or equal to i/m and “k” is set  
23 to be (i mod m). Then a decision is made depending on the value of the “k”. This decision is  
24 made by having the value of “k” compared with all possible values it can take, i.e., 0 to m-1 in  
25 steps (421), (422), ..., (42m) respectively. Based on the success of this comparison exactly one  
26 of steps (431), (432), ..., (43m) is taken where a success in comparison (421) leads to step (431)  
27 and so on and finally a success in comparison (42m) leads to step (43m). Steps (431), (432), ...,  
28 (43m) of which only one is performed are quite similar. In step (431) variables “T1”,.., “Tm” are  
29 set to be the first (b/m) bits of U1[j],...,Um[j] respectively. In step (432) the variables “T1” ,..,

1 “T<sub>m</sub>” are set to be the second (b/m) bits of U<sub>1</sub>[j],...,U<sub>m</sub>[j] respectively and so on and in step  
2 (43m) the variables “T<sub>1</sub>”,..., “T<sub>m</sub>” are set to be the last (b/m) bits of U<sub>1</sub>[j],...,U<sub>m</sub>[j] respectively.  
3 After performing any one of the steps (431), (432), ..., (43m), step (410) is performed which  
4 computes the value of T[i] to be the concatenation of the first (b/m) bits from each of the  
5 variables “T<sub>1</sub>”,..., “T<sub>m</sub>”.

6 Whereas the above descriptions showed how to create and use split tables of equal size, it is easy  
7 to modify these constructions to produce tables of unequal size. In an example embodiment, the  
8 “**Unequal Table Split Method**” is used in which the lookup table T is split into k tables  
9 T<sub>1</sub>,..,T<sub>k</sub> wherein each table T<sub>i</sub> is a compacted table containing information only about b<sub>i</sub> bits of  
10 the data values of T, and where the b<sub>i</sub>’s (for i=1 to k) sum upto b and are not all equal. This  
11 results in tables T<sub>1</sub>,..,T<sub>k</sub> being of different sizes.

12 Those with ordinary skill in the art will recognize that the methods presented herein are most  
13 advantageous when the index size of the table being split can be represented by a power of 2.  
14 However it is noted that the concepts of the present invention are applicable to any index size.  
15 Indeed even the examples presented herein are not limited to tables with index sizes represented  
16 by a power of 2.

### 17 *The Table Mask operation.*

18 The table mask operation takes a known or split table n-bit to b-bit T and creates a masked table  
19 T’ in RAM having the same table size with the property that it is feasible to perform the table  
20 lookup operation of T using only T’. The table T’ has a randomness property in that each data  
21 entry in it is statistically independent of any of the entries T. In addition if a table lookup  
22 operation of a particular index of T being performed using only T’ then the index or indices  
23 looked up in T are statistically independent of the said particular index of T. The Table Mask  
24 operation provides a strong defense against side-channel attacks. This is because if an  
25 implementation directly looks up the known table T, then the side-channel will correlate to each  
26 bit of the table index accessed and to each bit of the value of the table entry at that index. This

1 fact can be exploited by an attacker who knows T. However, if T' is used instead of T then the  
2 side channel will correlate to the bits of the index and data accessed in T' which is random and  
3 statistically independent of T and thus provides no useful information to the attacker.  
4 Implementation of the Table mask can be accomplished in a variety of ways known to those  
5 skilled in the art becoming familiar with the spirit and concepts presented herein.

6 One advantageous way to perform table lookup, is herein referred to as the "**Input-Output**  
7 **Permutation Masking**" method. The Input-Output Permutation Masking method is done as  
8 follows:

9 In what follows, without loss of generality assume that the indices in T has N distinct indices  
10 which vary from 0 to N-1.

11 Let IP (index permutation) be a class of n-bit to n-bit permutations with the property that for any  
12 n-bit value i, if a permutation ip is chosen uniformly at random from the class IP, then the value  
13 ip(i) is statistically independent of i.

14 Let OP (output permutation) be a class of b-bit to b-bit permutations with the property that for  
15 any b-bit value o, if a permutation op is chosen uniformly at random from the class OP, then the  
16 value op(o) is statistically independent of o.

17 For each instance of a operation needing one or multiple lookups of a table T, a fresh random  
18 looking "masked" table T' is computed and placed in RAM. This is done as follows:

19  
20 Choose a permutations  $ip \in IP$  uniformly at random from that class.

21 Choose a permutation  $op \in OP$  uniformly at random from that class.

22 Define the masked table T' as follows.

1 For all indices  $i$  of the table  $T$ ,  $i \leq 0 < N$ ,  $T'[ip(i)] = op(T[i])$ .  
2 The table lookups thus works with masked values of the index ( $ip(i)$  instead of  $i$ ) and result in  
3 masked values of the output. By working throughout with appropriately masked values, one can  
4 perform the entire algorithm without ever exposing any intermediate result in the clear and  
5 preventing a side-channel attack. Working with masked values is a well known mechanism to  
6 avoid side-channel attacks and has been extensively described in the literature. For example, this  
7 is shown in, S. Chari, C. Jutla, J.R. Rao, P. Rohatgi, “Towards Sound Approaches to Counteract  
8 Power-Analysis Attacks”, CRYPTO ’99 Conference, LNCS 1666, Aug 1999, CHANGE TO AS  
9 DISCUSSED IN BACKGROUND.

10 To further illustrate the Table Mask operation we provide a general flowchart of how  $T'$  is  
11 obtained from  $T$  and how lookups of  $T$  is performed using only  $T'$  based using the Input-Output  
12 Permutation Masking Method. Later another Table Masking method herein referred to as the  
13 “**Input-Output XOR Permutation Masking Method**” will be described in detail. This is  
14 similar to the Input-Output Permutation Masking Method but instead of using general  
15 permutation, XOR based permutations are used. That method will also be used in an  
16 advantageous embodiment.

17 Figure 5 shows a flow chart for computing  $T'$  from  $T$  using the Table Mask operation based on  
18 the Input-Output Permutation Masking Method. As a first step (500) two random permutations  
19 “ip” and “op” are chosen uniformly at random from the sets IP and OP respectively. In the next  
20 step (501), a loop variable “ $i$ ” is set to 0. Labels (502), (503) and (505) show how this flowchart  
21 implements a loop where the variable “ $i$ ” varies from 0 to  $N-1$ . Step (502) is a comparator which  
22 checks that ( $i < N$ ) and if so continues processing at step (504) otherwise it stops the processing  
23 (503). After the processing step (504) the loop variable “ $i$ ” is incremented at step (505) and  
24 control is transferred again to the loop range check (502). The main processing for each “ $i$ ” in the  
25 range is done in step (504), where  $T'[ip(i)]$  is set to  $op(T[i])$ . This completes the description of  
26 the flowchart to compute  $T'$  from  $T$ .

1 Figure 6 shows a flow chart for using the table  $T'$  created in Figure 5 using the Input-Output  
2 Permutation Masking Method for performing table lookups in table  $T$ . Suppose it is desired to  
3 lookup  $T[i]$  using  $T'$ . A first step (600) is to compute a variable “ind” to be  $ip(i)$ . The variable  
4 “mvalue” is then obtained by looking up  $T'$  at index of “ind”. The variable “result” is set to the  
5 inverse permutation of “op” (that is  $op^{-1}$ ) applied to “mvalue”. The value of  $T[i]$  is the same as  
6 “result” (601). It should be noted here that the table  $T'$  is looked up at a random permutation of  
7 the index  $i$  and the value which is looked up is a random permutation of the value of  $T[i]$ . This  
8 means that both the index and value looked up in  $T'$  is statistically independent of  $i$  and  $T[i]$   
9 respectively.

10 In some scenarios it is advantageous to use simple XOR based permutations for IP and OP. This  
11 is the motivation for the Input-Output XOR Permutation Masking Method. Choosing a n-bit to  
12 n-bit XOR permutations (such as “ip”) consists of choosing a single n-bit random number “r1”  
13 and the XOR permutation “ip” defined by “r1”, just XORs its input with “r1”. Similarly choosing  
14 a b-bit to b-bit XOR based permutation for “op” consists of choosing a single b-bit random  
15 number “r2”. Figure 7 gives a flowchart for computing  $T'$  from  $T$  using the Table Mask  
16 operation based on the Input-Output XOR Permutation Masking Method. As a first step (700) a  
17 random XOR index permutation is chosen by choosing a random n-bit number “r1” and a  
18 random XOR output permutation is chosen by choosing a random b-bit number “r2”. In the next  
19 step (701), a loop variable “i” is set to 0. Labels (702), (703) and (705) show how this flowchart  
20 implements the loop where the variable “i” varies from 0 to  $N-1$ . Step (702) is a comparator  
21 which checks that  $(i < N)$  and if so continues processing at step (704) otherwise it stops the  
22 processing (703). After the processing step (704) the loop variable “i” is incremented by 1 at step  
23 (705) and control is transferred again to the loop range check (702). The main processing for  
24 each “i” in the range is done in step (704), where  $T'[i \text{ xor } r1]$  is set to  $(T[i] \text{ xor } r2)$ . This  
25 completes the description of the flowchart to compute  $T'$  from  $T$ .

26 Figure 8 shows a flow chart for using the table  $T'$  created in Figure 7 using the Input-Output  
27 XOR Permutation Masking Method for performing table lookups in table  $T$ . Suppose it is desired  
28 to lookup  $T[i]$  using  $T'$ . A first step (800) is to compute a variable “ind” to be  $(i \text{ xor } r1)$ . The

1 variable "mvalue" is then obtained by looking up  $T'$  at index of "ind". The variable "result" is set  
2 to ( mvalue xor r2). The value of  $T[i]$  is the same as "result" (801).

3 **Problems with Table Mask**

4 The main problem with the "Table Mask" building block described above is that it needs table  $T'$   
5 to be in RAM and the size of  $T'$  is *the same as that of*  $T$ . In many cases such a large amount of  
6 RAM may not be available. Additionally, if many such tables have to be examined multiple  
7 times within the algorithm, then for efficiency purposes, masked versions of all of them should  
8 be simultaneously kept in RAM. Also, if  $n$  is large, then it may not be possible to easily index  
9 directly into  $T'$  (or  $T$  for that matter) and the index space would have to be split into multiple  
10 tables, opening up an avenue for attacks since the attacker may be able to discern which of the  
11 multiple tables was accessed which in turn gives information about the supposedly secret value  
12 of the index.

13 The solution to all these problems, is to use the Table Mask operation in conjunction with the two  
14 other operations, the Table Split operation which we described earlier and the Table Aggregate  
15 operation which we describe below. The Table Split operation takes care of large table sizes or  
16 tables with large index sizes. The Table Mask operation provides defense against side-channel  
17 attacks but requires as much RAM as the Table or Tables being accessed. In embodiments where  
18 there is enough available RAM and there is no problem of large table index, just a Table Mask  
19 operation suffices. In embodiments where there is enough available RAM but at least one Table  
20 has a problem of large index size, a combination of Table Split and Table Mask is usually  
21 enough to provide side-channel resistance. However, where available RAM is less than the  
22 combined sizes of the Tables to be protected, then either a combination of Table Mask operations  
23 and Table Aggregate operations is performed or a combination of all three operations, Table  
24 Split, Table Mask and Table Aggregate is performed.

25 **The Table Aggregate operation**

1 Suppose we have  $m$ , tables  $V_1, V_2, \dots, V_m$  each of size no more than  $M$  bytes. The Table  
2 Aggregate operation combines the given tables  $V_1, V_2, \dots, V_m$  to create an aggregate table  $W$  of  
3 size no more than  $M$  bytes with the property that given  $W$  and all but one of the tables  $V_i$ , it is  
4 feasible to recover the table  $V_i$ . The combination of the given tables to create the aggregate table,  
5 i.e., the Table Aggregate operation can be accomplished in a variety of ways as known to those  
6 skilled in the art becoming familiar with the spirit and concepts presented herein.

7 In one advantageous embodiment, hereinafter referred to as the "**Entry-wise Algebraic**  
8 **Aggregate Method**", the Table Aggregate operation is accomplished by combining  
9 corresponding data entries of the tables  $V_1, \dots, V_m$  using an algebraic operation to create an  
10 entries of the aggregate table  $W$ . Depending on the types of data values in the tables  $V_1, \dots, V_m$ ,  
11 there can be a variety of algebraic operators as known to those skilled in the art. Examples  
12 include the xor operation, the modular addition operator, the modular subtraction operation, etc.

13 This embodiment is particularly suitable if data entries of all tables are of similar size. An  
14 example of application of the Entry-wise Algebraic Aggregate Method is given in Figure 9  
15 where data values from  $m$  tables  $V_1, \dots, V_m$  having same index size  $N$  are combined to form a  
16 single table  $W$  having an index size of  $N$  using some algebraic operation "opn". As a first step  
17 (900) a loop variable "i" is set to 0. Labels (901), (902) and (904) show how this flowchart  
18 implements the loop where the variable "i" varies from 0 to  $N-1$ . Step (901) is a comparator  
19 which checks that  $(i < N)$  and if so continues processing at step (903) otherwise it stops the  
20 processing (902). After the processing step (903) the loop variable "i" is incremented at step  
21 (904) and control is transferred again to the loop range check (901). The main processing for  
22 each "i" in the range is done in step (903), where the  $i$ 'th data value of  $W$ , that is  $W[i]$ , is set to  
23 be the algebraic operation "opn" applied to the  $i$ 'th data values of  $V_1, \dots, V_m$ , i.e.,  $V_1[i]$ ,  
24  $V_2[i], \dots, V_m[i]$ . This completes the description of the flowchart to compute  $W$  from  $V_1, \dots, V_m$ .

25 Figure 10 shows how one can use the aggregate table  $W$  constructed in Figure 9 to look up an  
26 entry in any of the tables  $V_1, \dots, V_m$ , for example the entry  $V_1[i]$ , from  $W$  and the other tables ,  
27 i.e., how to look up the entry  $V_1[i]$  using only the tables  $W, V_2, \dots, V_m$ . In step (1000) first the a  
28 variable "agvalue" is set to  $W[i]$ , i.e., the aggregated value in  $W$  at index  $i$ . Then the values of  
29  $V_2[i], \dots, V_m[i]$  which were used in the aggregation operation in Figure 9 are looked up. Clearly,

1 the value of the variable “agvalue” was obtained by applying the algebraic operation “opn” to the  
2 values V1[i],..,Vm[i] in Step ( 903 ) of Figure 9. Therefore by using the inverse of the algebraic  
3 operation “opn”, a unique value for a variable “X” is determined such that (agvalue = opn(X,  
4 V2[i],...,Vm[i]) ). The value of “X” must be the value of V1[i] (1001).

5 In another advantageous embodiment, hereinafter referred to as the “**Byte-wise XOR Aggregate**  
6 **Method**”, W is created by padding with extra 0’s all tables V1,..,Vm to size M bytes and then  
7 doing a byte-wise XOR of the corresponding bytes in all the m padded tables. Clearly, a table Vi  
8 can be recovered from W and V1,..,Vi-1, Vi+1, ...Vm by XORing all these tables. Another  
9 embodiment uses byte-wise addition modulo 256 instead of XOR. The main advantage of using  
10 the byte-wise XOR or addition modulo 256 operation to create the aggregate table W is that, if  
11 the tables V1,...,Vm are created one or a few bytes at a time, then the table W is created using  
12 only slightly more than M bytes of memory.

13 As a further example, Figure 11 shows the process which combines data values from 2 tables  
14 V1,V2 having of size N bytes to form a single table W of size N bytes using the Byte-wise  
15 XOR Aggregate Method. In the following descriptions, the notation T.i will be used to denote the  
16 i’th byte of a Table T.

17 As a first step (1100) a loop variable i is set to 0. Labels (1101), (1102) and (1104) show how  
18 this flowchart implements the loop where the variable i varies from 0 to N-1. Step (1101) is a  
19 comparator which checks that i < N and if so continues processing at step (1103) otherwise it  
20 stops the processing (1102). After the processing step (1103) the loop variable i is incremented at  
21 step (1104) and control is transferred again to the loop range check (1101). The main processing  
22 for each i in the range is done in step (1103), where the i’th byte e of W, that is W.i is set to be  
23 V1.i XOR V2.i. This completes the description of the flowchart to compute W from V1,V2.

24 Figure 12 shows the Process which recovers the byte V1.i from the table W built in Figure 11  
25 using the Byte-wise XOR Aggregate method and the table V2. In step (1200) the variable  
26 “agvalue” is set to the aggregated byte value W.i. Then a variable “result” is computed as is (

1 agvalue XOR V2.i ). Clearly, since the value of “agvalue” was obtained by computing V1.i  
2 XOR V2.i in the construction of W, the value of the variable “result” must be the value of V1.i  
3 (1201).

4 This completes the description of the building blocks. Next, a method of using these building  
5 blocks to solve the problem of side-channel attacks on table lookups is described.

6 Suppose there are M bytes of available RAM to spare for table lookup on a device and a  
7 restriction on the memory addressing mechanism which limits any index to be no more than  
8 n-bits. Suppose there is at least one and potentially several known tables to be looked up in a  
9 side-channel attack resistant manner. The present invention solves this problem by using a  
10 combination of some of the building blocks Table Split, Table Mask and Table Aggregate  
11 described earlier. Since the Table Mask operation provides primary defense against side-channel  
12 attacks, it is used in most embodiments whereas the use of the operations Table Split and Table  
13 Aggregate is not necessary in some embodiments. As a first step the Table split operation is  
14 applied on all known tables whose lookup needs to be protected against side-channel attacks and  
15 whose table size is more than M and/or whose index size exceed the memory addressing  
16 mechanism. If there is no such known table then the Table split operation is not necessary.  
17 Applying the Table Split operation on any known table yields a collection of split tables whose  
18 table size is less than M and whose index size is within the n-bit limit As described earlier in the  
19 description of the Table Split operation and also in Figures 2 and 4, any access to any of the  
20 known tables which have been split can be substituted by appropriate accesses to the  
21 corresponding collection of split tables. Thus the implementation of table lookups is rewritten  
22 using these split tables. If these split tables were to be kept in ROM the implementation would  
23 be vulnerable to side channel attacks.

24 To take care of the side-channel attacks, in the next stage, the Table Mask operation is  
25 conceptually applied on all the split tables and also the remaining known tables that were not  
26 split to create a collection of masked tables. As described earlier, the masked tables have a  
27 randomness property, in that data values and corresponding indices to the masked tables are

1 statistically independent of the data values and corresponding indices of the tables upon which  
2 the Table Mask operation is performed. As described in detail in the section on Table mask  
3 operation and further described in Figures 6 and 8, all access to the known or split tables that  
4 have been masked can be replaced by accesses to these masked tables.

5 If all the masked tables together require no more than  $M$  bytes of RAM, then a side-channel  
6 attack resistant implementation within the constraints has already been obtained. In several  
7 embodiments, however, the total size of all masked tables still exceeds the limit  $M$  on available  
8 RAM, since it was only required that each individual table that is masked be of size no more than  
9  $M$  (otherwise it would have been split) and if there are several such tables, collectively the  
10 masked tables could require more RAM than  $M$ , since each masked table uses as much RAM as  
11 the size of the table that was masked. To take care of this problem, the Table aggregate  
12 operation is “conceptually applied” on some groups of the masked tables so that no more than  
13  $M$  bytes of RAM are consumed by the Aggregate tables thus produced or by the remaining  
14 masked tables not involved in any Aggregate operation. It should be noted that the randomness  
15 property of the masked tables is also maintained by the aggregated tables.

16 In practice, in embodiments where Table Aggregate is needed, the implementation may not even  
17 be able to actually create the full masked tables, since this could take much more RAM than is  
18 available. That is why it is stated that the Table Mask operation is “conceptually applied”. In  
19 embodiments where it is not possible to create the full masked tables due to available RAM  
20 constrains, the implementation would create one or a few bytes of these masked tables at a time  
21 and update the Aggregate table being computed. That is why, both in the description of the  
22 process to compute Table Mask, the data entries in the masked table are computed one at a time  
23 and in the description of the Table Aggregate, operation each data entry of the Aggregate table  
24 depends on one or at most a few of the data entries from each of the tables being aggregated.  
25 Using this approach the RAM usage would mostly be the  $M$  bytes needed to store the Aggregate  
26 tables and other masked tables not involved in an Aggregate operation. All known and/or split  
27 tables which were used for the Table Mask operation are put in ROM and all the tables in RAM,  
28 whether they be masked tables or Aggregate tables are hereinafter referred to as random tables.

1 With this infrastructure in place any data processing operation that required table lookup of any  
2 of the known tables can be implemented in a side-channel attack resistant manner using only the  
3 available RAM and memory addressing limits. Figure 13 summarizes this process to set up the  
4 infrastructure to be able to perform table lookups of one or more known lookup tables, each of  
5 these known lookup tables having a particular table size and a particular table index size, in a  
6 side-channel attack resistant manner with the constraints of M bytes of available RAM and a  
7 limit on addressing capability. For each particular known table first a check is made as to  
8 whether its particular table size is more than M OR its particular table index size is more than  
9 the addressing capability (1300). If this check passes this particular table needs to be split, it is  
10 declared splittable in step (1301). Otherwise, this particular table goes to the table mask stage  
11 (1303). If a particular table is declared splittable in step (1301) then this table is split into a  
12 collection of split tables in step (1302) and these split tables are then sent to the table mask stage  
13 (1303). At stage (1303) all tables whether they are split tables or known tables are masked using  
14 the Table Mask operation to yield a collection of masked tables, where each of these masked  
15 tables has a randomness property. As described earlier, in practice this masking operation may  
16 only be done conceptually, i.e., done in conjunction with the table aggregate operation (1304).  
17 Some groups of masked tables are aggregated in step (1304) if needed, e.g., all masked tables  
18 cannot fit in available RAM to yield a collection of Aggregate Tables in RAM. With the  
19 collection of known and split tables (tables which were masked) in ROM and the Aggregate and  
20 remaining masked tables in RAM, i.e., a collection of random tables, any data processing  
21 operation which required any lookup of any of the known tables can be performed in a  
22 side-channel resistant manner. This completes the summary presented in figure 13.

23 Now we provide additional details as to how the infrastructure consisting of the known and split  
24 tables that were masked being in ROM and the aggregate and remaining masked tables in RAM  
25 are used to any perform data processing operation which requires a lookup of any of the known  
26 tables. Suppose an index I into a particular known table P needs to be looked up in a side-channel  
27 resistant manner. If the known table was split during setup, then the problem can be solved if  
28 several indices can be looked up into split tables as described the description of the Table Split  
29 operation and in particular Figures 2 and 4. Since all the split tables and all the known tables that

1 were not split were masked, the problem of looking up  $P[I]$  can be solved if any index in any  
2 table that was involved in the masking step can be looked up. Note that in the setup, all the split  
3 tables and the tables which were not split are in ROM, but these cannot be directly used since the  
4 direct access will open up side-channel exposures. To get side-channel resistance the random  
5 tables, i.e., the masked or aggregate tables in RAM, which are random and statistically  
6 independent of the known and split tables will have to be used. So the problem reduces to that of  
7 accessing any index  $L$  in any of the table  $R$  which is in ROM using the masked tables or the  
8 aggregate tables instead of the ROM table. In the case where  $R$  which is in ROM needs to be  
9 accessed and the  $R'$ , masked version of the table  $R$ , is available as a random table in RAM, the  
10 problem is solved as shown in the description of the Table Mask operation and in particular  
11 figures 6 and 8.. Essentially the problem is reduced to looking up an entry  $T$  of  $R'$  which can be  
12 done directly if  $R'$  is available. In the case where  $R'$  has been aggregated into an aggregate table  
13  $W$  then the description of the Table Aggregate operation and in particular figures 10 and 12 show  
14 that the problem obtaining  $R'[T]$  from the aggregate table  $W$  reduces to the problem of lookup of  
15 an Aggregate table entry (which is done directly) and looking up certain entries and one or more  
16 other masked tables,  $V'1, \dots, V'm$ . Since the unmasked versions of all these masked tables say  
17  $T1, \dots, Tm$  are in ROM, using the description of the Table Mask operation, specifically Figures 5  
18 and 7 which shows how masked tables are generated, one can obtain the values of entries in  
19  $V'1, \dots, V'm$  using DIRECT accesses to tables  $T1, \dots, Tm$  in ROM. Since the data values and  
20 indices in tables  $V'1, \dots, V'm$  are generated to be statistically independent of the values and  
21 indices in tables  $R'$  or  $R$  or  $T1, \dots, Tk$ , this DIRECT access to  $T1, \dots, Tk$  leaks no information on  
22 the side-channel since the indices accessed and data values obtained are statistically independent  
23 of  $R$  and  $L$ . Thus the problem of obtaining  $R'[T]$  from the aggregate table in a side-channel  
24 resistant manner is solved which in turn solves the problem of obtaining  $R[L]$  which in turn  
25 solves the original problem obtaining  $P[I]$  in a side channel resistant manner.

26 For illustrative purposes we now describe an example of this process of using the infrastructure  
27 to build and to do a known table lookup operation. In the example, a n-bit to 8-bit lookup Table  
28  $T$  with index size  $2^n$  and table size  $2^n$  has to be implemented on a device with available  
29 memory of roughly  $2^n/2$  bytes and an memory accessing mechanism which restricts index sizes

1 to be  $2^n/2$ . The infrastructure to do this is straightforward using this invention. First the  
2 Two-way Byte Table Splitting method is directly applied to T, as shown in Figure 1 and  
3 described in detail earlier. This yields two  $n-1$  bit by 8-bit split tables U1 and U2, each of size  
4  $2^n/2$  bytes and index size  $2^n/2$ . Then the process of Table masking is “conceptually applied” to  
5 the tables U1 and U2 to conceptually yield the tables U1’ and U2’. U1’ and U2’ are the same  
6 size as U1 and U2. In each case, the Input-Output XOR Permutation Masking Method is used  
7 for the Table Mask operation as shown in Figure 7. Let r1 and r2 be the index and output XOR  
8 masks used for the masking operation that yielded U1’ from U1 and let s1 and s2 be the index  
9 and output XOR masks used for the masking operation that yielded U2’ from U2. In practice  
10 U1’ and U2’ are not actually computed completely, but are computed byte by byte and used to  
11 compute an aggregate table W using the Byte-wise XOR Aggregate method as described earlier  
12 and as shown in Figure 11. The table W, which is of size  $2^n/2$  and index  $2^n/2$  is kept in RAM and  
13 the tables U1 and U2 are kept in ROM. This completes the description of how the random table  
14 W and the split tables U1 and U2 are set up. Next the mechanism to access any entry of T, say  
15 T[i] in a side-channel attack resistant manner is described. This process is also illustrated in  
16 Figure 14. As explained in the description of the Two-way Byte Table Splitting Operation and  
17 further illustrated in Figure 2 in step (201) and in steps (202) or (203), computing T[i] requires  
18 access to the bytes U1[j] and U2[j] where the variable “j” is (i div 2). Now as explained in the  
19 description of the Input-Output XOR Permutation Method and further illustrated in Figure 8, step  
20 (800) computing U1[j] needs access to U1'[j xor r1]. Similarly computing U2[j] needs access to  
21 U2'[j xor s1]. Since U1’ and U2’ are not available and only the aggregate table W is available, as  
22 explained in the description of the Byte-wise XOR Aggregate method, obtaining U1'[j xor r1],  
23 needs access to W[j xor r1] as shown in Figure 12, step (1200) and obtaining U2'[j xor s1] needs  
24 access to W[j xor s1]. Since W is available this step can be performed directly. However,  
25 according to step (1200), obtaining U1'[j xor r1] from W[j xor r1] also needs access to U2'[j  
26 xor r1] and obtaining U2'[j xor s1] from W[j xor s1] also needs access to U1'[j xor s1] and the  
27 tables U1’ and U2’ are not available in ROM or RAM. However, the tables U1 and U2 from  
28 which U1’ and U2’ were derived in the Table mask operation are in ROM. Therefore by  
29 repeating the steps used to create entries in U1’ and U2’ using U1 and U2 based on the

1 Input-Output XOR Permutation Method as illustrated in Figure 7, the values  $U2'[j \text{ xor } r1]$  and  
2  $U1'[j \text{ xor } s1]$  can be obtained. For example, as explained in the description of the Input-Output  
3 XOR Permutation Method and in Figure 7 step (704), for any  $i$ , the data value  $(U1'[i \text{ xor } r1])$  is  
4  $(U1[i] \text{ xor } r2)$ . Thus, the value  $U1'[j \text{ xor } s1]$  which is the same as  $U1'[ (j \text{ xor } s1 \text{ xor } r1) \text{ xor } r1 ]$   
5 must be the same as  $U1[(j \text{ xor } s1 \text{ xor } r1)] \text{ xor } r2$ . Thus the value  $U1'[j \text{ xor } s1]$  is obtained by an  
6 access to  $U1[j \text{ xor } s1 \text{ xor } r1]$  and similarly the value of  $U2'[j \text{ xor } r1]$  is obtained by an access to  
7  $U2[j \text{ xor } r1 \text{ xor } s1]$ . Based on the description presented above, Figure 14 describes the steps  
8 needed to lookup  $T[i]$  in a side-channel attack resistant manner using the aggregate table  $W$  and  
9 the tables  $U1$  and  $U2$ . As a first step (1400), the variable “ $j$ ” is set to  $(i \text{ div } 2)$ , the variable “ $k1$ ” is  
10 set to  $(j \text{ xor } r1)$  the variable “ $k2$ ” is set to  
11  $(j \text{ xor } s1)$  and the variable “ $k$ ” is set to  $(j \text{ xor } r1 \text{ xor } s1)$ . In the next step (1401), the table  $W$  in  
12 RAM is accessed, with the variable “ $amval\_low$ ” being set to  $W[k1]$  and the variable  
13 “ $amval\_hi$ ” being set to  $W[k2]$ . Subsequently, in the next step (1402), the tables  $U1$  and  $U2$  in  
14 ROM are accessed, with the variable “ $mres\_lo$ ” being set to  $(amval\_low \text{ xor } U2[k])$  and the  
15 variable “ $mres\_hi$ ” being set to  $(amval\_hi \text{ xor } U1[k])$ . The unmasking is done in step (1403),  
16 where the variable “ $res\_lo$ ” is set to  $(mres\_low \text{ xor } r2 \text{ xor } s2)$  and the variable “ $res\_hi$ ” is set to  
17  $(mres\_hi \text{ xor } s2 \text{ xor } r2)$ . From the definitions, it is easy to check that “ $res\_lo$ ” and “ $res\_hi$ ” are  
18 indeed equal to the values of  $U1[j]$  and  $U2[j]$ . The rest of the process is just a reconstruction of  
19  $T[i]$  using the values  $U1[j]$  and  $U2[j]$  where “ $j$ ” is  $(i \text{ div } 2)$ . First a check is made whether “ $i$ ” is  
20 even or odd (1404) by checking whether or not  $(i \text{ mod } 2)$  is 0. If “ $i$ ” is even, then in step (1405),  
21 a variable “ $a$ ” is set to the first nibble of “ $res\_lo$ ” and the variable “ $b$ ” is set to be the first nibble  
22 of “ $res\_hi$ ” and a byte sized variable “ $result$ ” is assigned to have its first nibble as “ $a$ ” and  
23 second nibble as “ $b$ ”. It is easy to check the “ $result$ ” equals  $T[i]$  in this case. In the case where “ $i$ ”  
24 is odd, then in step (1406), a variable “ $a$ ” is set to the second nibble of “ $res\_lo$ ” and the variable  
25 “ $b$ ” is set to be the second nibble of “ $res\_hi$ ” and a byte sized variable “ $result$ ” is assigned to have  
26 its first nibble as “ $a$ ” and second nibble as “ $b$ ”. It is easy to check the “ $result$ ” equals  $T[i]$  in this  
27 case as well. Thus in either case, the value of  $T[i]$  is the same as the value of “ $result$ ” and can be  
28 assigned this value in step (1407). Thus we get a side-channel resistant implementation  
29 involving table lookups within the resource/addressing bounds.

1 Whereas, the exposition, thus far, was meant to provide a general description of how the  
2 invention would work for a wide variety of situations in which it is applicable, its full generality  
3 may not be obvious to those with only ordinary skill in the art. Therefore here we will explicitly  
4 point out some additional features and applications of this invention which we believe may not  
5 have been obvious to those with only ordinary skill in the art.

6 The assumption in the definition of the Table Mask operation that the indices to the masked table  
7 are masked by a single permutation and the output is masked by a single permutation has been  
8 made here for the purposes of clarity of exposition. As such this provides a countermeasure  
9 against first-order side-channel attacks. It is expected that those skilled in the art will be aware  
10 of more powerful attacks known in the literature as higher order side-channel attacks. Those  
11 skilled in the art will easily recognize that, in the Table Mask operation, in practice, the  
12 permutation for the index could be formed by composing several individual permutations and  
13 the output of the table could be masked by a permutation which is formed by composing several  
14 individual permutations. Those skilled in the art should also recognize upon reflection that the  
15 use of several individual permutations instead of a single permutations provides a generic  
16 mechanism to defeat higher-order side channel attacks and that this invention also provides the  
17 recipe for dealing with these more powerful attacks.

18 **ADVANTAGEOUS EMBODIMENT**

19  
20 The protected table lookup scheme (described above) implemented in terms of the table splitting,  
21 table masking and table aggregation primitives will be illustrated for the COMP128 algorithm..

22 The COMP128 algorithm performs lookups of tables of sizes 512, 256, 128 and 64 bytes. In  
23 many chipcards and other devices, the amount of available RAM available is very small and has  
24 to be used judiciously. In particular, tables such as those described above cannot be  
25 accommodated in RAM, due to constraints of space. While there may be sufficient  
26 ROM/EEPROM available for the tables, a straightforward implementation of tables using

1 ROM/EEPROM would leave the implementation vulnerable to side-channel attacks. Thus one  
2 has to resort to using the operations described above such as table splitting, table masking and  
3 table aggregation to implement tables in a protected manner on constrained memory devices.

4 For illustrative purposes, we describe how the 512 byte table of COMP128 which has 512  
5 byte-sized data values having an index ranging from 0 to 511 is implemented on chipcards with  
6 available RAM being just a few bytes more than 256 bytes in a side-channel attack resistant  
7 manner. The original 512 byte is shown below. The table consists of 32 rows of 16 data values  
8 each. Each value is a byte and is shown using the hexadecimal notation below:

9 66 b1 ba a2 02 9c 70 4b 37 19 08 0c fb c1 f6 bc  
10 6d d5 97 35 2a 4f bf 73 e9 f2 a4 df d1 94 6c a1  
11 fc 25 f4 2f 40 d3 06 ed b9 a0 8b 71 4c 8a 3b 46  
12 43 1a 0d 9d 3f b3 dd 1e d6 24 a6 45 98 7c cf 74  
13 f7 c2 29 54 47 01 31 0e 5f 23 a9 15 60 4e d7 e1  
14 b6 f3 1c 5c c9 76 04 4a f8 80 11 0b 92 84 f5 30  
15 95 5a 78 27 57 e6 6a e8 af 13 7e be ca 8d 89 b0  
16 fa 1b 65 28 db e3 3a 14 33 b2 62 d8 8c 16 20 79  
17 3d 67 cb 48 1d 6e 55 d4 b4 cc 96 b7 0f 42 ac c4  
18 38 c5 9e 00 64 2d 99 07 90 de a3 a7 3c 87 d2 e7  
19 ae a5 26 f9 e0 22 dc e5 d9 d0 f1 44 ce bd 7d ff  
20 ef 36 a8 59 7b 7a 49 91 75 ea 8f 63 81 c8 c0 52  
21 68 aa 88 eb 5d 51 cd ad ec 5e 69 34 2e e4 c6 05  
22 39 fe 61 9b 8e 85 c7 ab bb 32 41 b5 7f 6b 93 e2  
23 b8 da 83 21 4d 56 1f 2c 58 3e ee 12 18 2b 9a 17  
24 50 9f 86 6f 09 72 03 5b 10 82 53 0a c3 f0 fd 77  
25 b1 66 a2 ba 9c 02 4b 70 19 37 0c 08 c1 fb bc f6  
26 d5 6d 35 97 4f 2a 73 bf f2 e9 df a4 94 d1 a1 6c  
27 25 fc 2f f4 d3 40 ed 06 a0 b9 71 8b 8a 4c 46 3b  
28 1a 43 9d 0d b3 3f 1e dd 24 d6 45 a6 7c 98 74 cf

1 c2 f7 54 29 01 47 0e 31 23 5f 15 a9 4e 60 e1 d7  
2 f3 b6 5c 1c 76 c9 4a 04 80 f8 0b 11 84 92 30 f5  
3 5a 95 27 78 e6 57 e8 6a 13 af be 7e 8d ca b0 89  
4 1b fa 28 65 e3 db 14 3a b2 33 d8 62 16 8c 79 20  
5 67 3d 48 cb 6e 1d d4 55 cc b4 b7 96 42 0f c4 ac  
6 c5 38 00 9e 2d 64 07 99 de 90 a7 a3 87 3c e7 d2  
7 a5 ae f9 26 22 e0 e5 dc d0 d9 44 f1 bd ce ff 7d  
8 36 ef 59 a8 7a 7b 91 49 ea 75 63 8f c8 81 52 c0  
9 aa 68 eb 88 51 5d ad cd 5e ec 34 69 e4 2e 05 c6  
10 fe 39 9b 61 85 8e ab c7 32 bb b5 41 6b 7f e2 93  
11 da b8 21 83 56 4d 2c 1f 3e 58 12 ee 2b 18 17 9a  
12 9f 50 6f 86 72 09 5b 03 82 10 0a 53 f0 c3 77 fd  
13  
14  
15  
16  
17

13 Let us call the original 512 byte COMP128 table, table T. Clearly  $T: \{0,1\}^9 \rightarrow \{0,1\}^8$ , that is it  
14 takes a 9-bit index and yields an 8-bit output. The first version of the COMP128 algorithm is  
15 written assuming that the 512 byte table is resident in ROM but this is clearly susceptible to  
16 side-channel attacks. The present invention is then applied to convert the implementation to one  
17 which is resistant to side-channel attacks.

18 As a first step, since the table size of T, which is 512 bytes, exceeds the amount of available  
19 RAM which is just a few bytes more than 256, the Table T should be split. In this embodiment  
20 the Two-way Byte Table splitting method is applied to obtain two tables U1 and U2 where  
21  $U1: \{0,1\}^8 \rightarrow \{0,1\}^8$  and  $U2: \{0,1\}^8 \rightarrow \{0,1\}^8$ . Each of these tables takes an 8-bit index and  
22 produces an 8-bit output value. Note that each of U1 and U2 is 256 bytes in size. The resulting  
23 tables U1 and U2 are shown below. Each of the tables, U1 and U2, consists of 16 rows of 16 byte  
24 sized data values each. The byte values have been shown in hexadecimal notation.

1 Table U1:

2 16 2a c2 b0 97 c8 1b c6 5d 57 fa 3f 29 f4 41 1c  
3 5c f4 30 d6 09 1b ac 6b a3 dd 3f ed 46 56 c8 4f  
4 27 49 17 e1 3f 59 e0 17 36 cc 69 a4 08 b1 42 05  
5 a5 78 67 8a 3f ee da 09 ba 85 3b 4a 23 82 6c 90  
6 7d 8b ed 45 c4 76 2f 4c 58 0e d4 79 e0 73 7c 72  
7 5e 96 20 5c 09 41 de fd 6f 98 ab 19 a5 3f 81 20  
8 a8 b8 1d dd ec 49 4e 56 e9 b1 5e b7 2b 51 bf 23  
9 a8 13 6d cf e8 2e b8 7a f0 f6 29 b3 20 a3 03 7d  
10 61 a2 2c 0b 79 8c b1 6c d5 75 af f3 92 4f 14 c1  
11 c5 4f 03 6d 90 b1 ca b6 3a dd f3 de 64 65 8c f4  
12 72 94 71 1e f3 95 0e 71 63 cc 96 4a 80 1b 24 50  
13 5a 87 76 a8 f3 ee ad 90 ab 58 b3 a4 32 28 c6 09  
14 d7 b8 de 54 4c 67 f2 c4 85 e0 4d 97 0e 37 c7 27  
15 e5 69 02 c5 90 14 ed df f6 89 ba 91 5a f3 18 02  
16 8a 8b d1 dd ce 94 e4 65 9e 1b e5 7b b2 15 fb 32  
17 8a 31 d6 fc 8e e2 8b a7 0f 6f 92 3b 02 3a 30 d7

18 Table U2:

19 b6 ab 90 47 13 00 cf bf d6 39 42 7b fe da 9d a6  
20 2f 2f d4 e0 ab 78 84 43 14 90 b3 1d 2d 4a 79 7c  
21 cf 52 04 03 25 1a 46 ed fb 51 7c 40 8f 01 89 3f  
22 59 27 e5 e6 1a b7 8c b8 1f 26 ed 13 b3 d6 18 72  
23 63 4c 61 d5 cb b9 40 ca c3 09 26 09 d9 aa 83 ed  
24 aa f2 2e ed dd 4f bc f7 3e 5a 77 94 e7 68 c8 5c  
25 a6 e8 55 ac 5e 36 e2 0c f3 96 88 ac 3b b4 67 e9  
26 db 28 54 21 35 1e 21 19 95 68 70 50 81 05 fc 7f  
27 6b ba 09 74 31 00 fc fb 6d 93 24 b7 ef ad d9 6a

1 f2 f2 4d 0e ba 87 48 34 41 09 3b d1 d2 a4 97 c7  
2 fc 25 40 30 52 a1 64 de bf 15 c7 04 f8 10 98 f3  
3 95 72 5e 6e a1 7b c8 8b f1 62 de 31 3b 6d 81 27  
4 36 c4 16 5d bc 9b 04 ac 3c 90 62 90 9d aa 38 de  
5 aa 2f e2 de dd f4 cb 7f e3 a5 77 49 7e 86 8c c5  
6 6a 8e 55 ca e5 63 2e c0 3f 69 88 ca b3 4b 76 9e  
7 bd 82 45 12 53 e1 12 91 59 86 07 05 18 50 cf f7

8 Next, the table masking primitive to create masked versions V1 and V2 of U1 and U2  
9 respectively. In this embodiment, the Input-Output XOR Permutation method is “conceptually  
10 applied” to create the masked tables V1 and V2 from U1 and U2. Recall that the Input-Output  
11 XOR Permutation method works as follows: Let the symbol “ $\oplus$ ” denote the XOR operator.  
12 Pick two 8-bit random masks for each table, say r1 and r2 for table U1 (s1 and s2 for table U2  
13 respectively). The indices and entries of U1 (resp. U2) are masked by xor’ing them with r1 and r2  
14 (resp s1 and s2) respectively. That is  $V1[i \oplus r1] = U1[i] \oplus r2$ . Similarly for U2 and V2.

15 As an example, assume that for the masking of table U1, r1 = E4 and r2 = 8C. Also assume  
16 that for masking table U2, s1 = A5 and s2 = 3B.. The resulting masked tables V1 and V2 are  
17 shown below. Note that masking does not change the size of the table. Both V1 and V2 consist of  
18 16 rows of 16 byte-sized data values each. Each of the data values has been shown in  
19 hexadecimal notation.

20 Table V1:

21 42 18 68 e9 06 07 5d 51 3e 99 77 be 12 97 69 f7  
22 02 6e 07 2b 06 bd 5a 70 8e b6 bc 5b 83 e3 1e b7  
23 c0 eb 7e 48 5b 34 52 d8 82 bb 4b ab 09 6c c1 1b  
24 1c 98 61 53 69 e5 8e 49 d6 7f 94 8e 7a 05 36 1d  
25 7f 19 82 fd fe 18 fd 92 0c 97 a8 dc ef 40 1a c6  
26 7f 62 21 1c d6 0b fa 24 be a4 4a 85 27 d4 3f 28  
27 f5 00 3d e0 ed 2e a0 87 1e c3 98 4d 59 f9 23 7f

1 1c 3d 46 3a 49 c3 8f e1 e8 e9 00 78 b6 51 7f 52  
2 60 c5 c2 da 24 34 91 51 a7 dd 33 af 65 3d d2 3b  
3 64 a2 34 f6 24 9f e1 43 ac 2f 8f f1 7c 7a a5 3f  
4 48 fa a3 c0 f1 07 61 c9 6c ff f0 fe d4 82 58 f5  
5 85 cd 52 71 d2 1a ac d0 29 b3 0d ac e3 14 27 95  
6 b3 d5 6c 9b ab c5 9b 6d 84 3d ce 89 ba 40 e5 28  
7 b3 62 56 85 29 f4 eb 06 af 0e e0 1c 36 09 b7 c6  
8 1b 44 97 4a 9a a6 4e 3c a5 78 cd 90 d1 db 76 b3  
9 85 97 20 e7 d0 78 bc 5a ca da 44 c3 2f 51 b3 61

10 Table V2:

11 9a 69 e5 5f 1e c7 0b 7b 2b c3 c8 a3 2e 84 3f fc  
12 40 9a b0 f3 49 ae 55 65 56 00 1c ba 59 ca 0a e5  
13 3b 0a c0 c7 81 50 4f 32 96 d4 51 e2 a8 56 8c 1f  
14 bc 81 0f 73 c9 c9 35 76 9f e9 fc ac 32 7a ea 00  
15 58 de fb 15 b5 51 f1 6e 70 88 a5 4d 52 04 f1 b3  
16 da 68 aa 29 b9 86 29 7e 6b 23 cc f4 bd 62 3e 3c  
17 a0 87 97 3f ff 0d 66 2d 91 a6 e5 03 ab 07 ab 59  
18 cf e6 44 f0 14 91 e5 d9 bd 45 fe b7 9e d8 72 4c  
19 21 1e d6 7d 69 f4 38 3f 3a b4 04 b2 6a c0 7b 47  
20 8c 21 83 b7 1c 62 dd de ed 88 49 23 1d 24 28 d6  
21 3b 28 84 f4 90 8d 7c ab e1 c5 9d a6 02 ed 40 79  
22 43 90 78 bf 14 14 db ef 71 16 47 42 ab 2f 26 88  
23 0d 65 37 d9 d3 9d 97 6e 8f 00 d2 5c ad c8 97 b3  
24 25 0e 22 1a 13 e0 1a 6f 3e ba 44 c7 53 ae 6b 4b  
25 82 f0 f1 7b 77 58 ee 5a 91 e2 d6 b8 32 f8 32 1d  
26 74 e6 cc 87 c9 91 d6 15 53 dc 67 f3 61 05 af 4c

1 Since the tables V1 and V2 are each of size 256 bytes, together they will occupy 512 bytes of  
2 RAM. Since that is more than available RAM, a table aggregate operation is recommended. As  
3 a next step the table aggregation primitive to create an aggregate table W of size 256 bytes. In  
4 this embodiment this is done using the Byte-wise XOR Aggregate method. Using this method W  
5 is computed as  $W = V1 \oplus V2$ , i.e., W is the Byte-wise XOR of corresponding bytes of V1 and  
6 V2, i.e., for any i between 0 and 255,  $W[i] = V1[i] \oplus V2[i]$ . Note that the construction of table  
7 W can be done on a byte by byte basis in RAM. If V1 and V2 are computed on a byte by byte  
8 basis, i.e., the masking operation is “conceptually applied” then the entire construction of W  
9 from U1 and U2 does not need space larger than the size of each of the individual tables.

10 For illustrative purposes, the resulting table W is shown below. Note that table aggregation  
11 results in a table of the same size, that is, a table consisting of 16 rows of 16 byte-sized data  
12 values each. Once again, the data values are shown in hexadecimal notation.

13 Table W:

14 d8 71 8d b6 18 c0 56 2a 15 5a bf 1d 3c 13 56 0b  
15 42 f4 b7 d8 4f 13 0f 15 d8 b6 a0 e1 da 29 14 52  
16 fb e1 be 8f da 64 1d ea 14 6f 1a 49 a1 3a 4d 04  
17 a0 19 6e 20 a0 2c bb 3f 49 96 68 22 48 7f dc 1d  
18 27 c7 79 e8 4b 49 0c fc 7c 1f 0d 91 bd 44 eb 75  
19 a5 0a 8b 35 6f 8d d3 5a d5 87 86 71 9a b6 01 14  
20 55 87 aa df 12 23 c6 aa 8f 65 7d 4e f2 fe 88 26  
21 d3 db 02 ca 5d 52 6a 38 55 ac fe cf 28 89 0d 1e  
22 41 db 14 a7 4d c0 a9 6e 9d 69 37 1d 0f fd a9 7c  
23 e8 83 b7 41 38 fd 3c 9d 41 a7 c6 d2 61 5e 8d e9  
24 73 d2 27 34 61 8a 1d 62 8d 3a 6d 58 d6 6f 18 8c  
25 c6 5d 2a ce c6 0e 77 3f 58 a5 4a ee 48 3b 01 1d  
26 be b0 5b 42 78 58 0c 03 0b 3d 1c d5 17 88 72 9b  
27 96 6c 74 9f 3a 14 f1 69 91 b4 a4 db 65 a7 dc 8d  
28 99 b4 66 31 ed fe a0 66 34 9a 1b 28 e3 23 44 ae

1 f1 71 ec 60 19 e9 6a 4f 99 06 23 30 4e 54 1c 2d

2 The table W is kept in RAM whereas the tables U1 and U2 are kept in ROM.  
3 The side-channel attack resistant version of the COMP128 algorithm is now written to use the  
4 table W and tables U1 and U2 instead of T. Note that when the original algorithm looks up  
5 index i in the table T, the output T[i] is an 8-bit value. This lookup operation is replaced by a  
6 sequence of steps which use the tables W, U1 and U2 instead of T[i] but provide the same result.  
7 This is done as follows:

8 First  $j = i \text{ div } 2$  is computed. Clearly, T[i] can be computed using the values of U1[j] and  
9 U2[j], but that would still be vulnerable to side channel attacks since the index j is not  
10 randomized. Instead an alternative approach is used. First set  $k1 = j \oplus r1$  and  $k2 = j \oplus s1$ . Note  
11 that the output W[k1] is really the value  $V1[k1] \oplus V2[k1]$ . This value is the same as  $U1[k1 \oplus$   
12  $r1] \oplus r2 \oplus U2[k1 \oplus s1] \oplus s2$ . Using the fact that  $k1 = j \oplus r1$ , this value is the same as  $U1[j] \oplus$   
13  $r2 \oplus U2[k1 \oplus s1] \oplus s2$ . The algorithm can use the original table U2 (stored in ROM/EEPROM)  
14 to get the value of  $U2[k1 \oplus s1]$ , xor this value with the  $U1[j] \oplus r2 \oplus U2[k1 \oplus s1] \oplus s2$  to get  
15  $U1[j] \oplus r2 \oplus s2$ . The masks r2 and s2 can then be removed by xoring to yield  $U1[i]$ . A similar  
16 process is followed to yield  $U2[j]$ . Depending on whether the value of  $(l \bmod 2)$  is 0 or 1, the first  
17 or second half of the bytes of  $U1[j]$  and  $U2[j]$  are retrieved and concatenated to return the value  
18 of the table lookup T[i]. In an actual implementation of COMP128, for defense against  
19 side-channel attacks, it is not advisable to compute unmasked values of  $U1[j]$  and  $U2[j]$  or  $T[i]$   
20 but it is acceptable to compute these values masked by known random values. Thus in this  
21 embodiment when the XOR masks of r2 and s2 are removed from the masked value of  $U1[j]$  or  
22  $U2[j]$  and additional known random mask R1 and R2 can be simultaneously applied, i.e., the  
23 values computed will be  $U1[j] \oplus R1$  and  $U2[j] \oplus R2$ . This can be accomplished, for example,  
24 if the unmasking of  $U1[j] \oplus r2 \oplus s2$  is done by first XOR masking with R1 and then removing  
25 the masks r2 and s2 using XOR. Using the masked values of  $U1[j]$  and  $U2[j]$  in the calculation of  
26  $T[i]$  will again result in a masked value of  $T[i]$ , i.e., the result will be  $T[i] \oplus R3$  where R3 is  
27 another known random mask related to R1 and R2.

1 In the description of the invention, thus far, an assumption has been made in the definition of the  
2 Table Mask operation that the indices to the masked table are masked by a single permutation  
3 and the output is masked by a single permutation. This assumption was made solely for the  
4 purposes of clarity of exposition as should not be viewed as limiting requirement for this  
5 invention. As such, the above description of the present invention provides a countermeasure  
6 against first-order side-channel attacks. It is expected that those skilled in the art will be aware  
7 of more powerful attacks known in the literature as higher order side-channel attacks. Those  
8 skilled in the art will easily recognize that, in the Table Mask operation, in practice, the  
9 permutation for the index could be formed by composing several individual permutations and  
10 the output of the table could be masked by a permutation which is formed by composing several  
11 individual permutations. Those skilled in the art should also recognize upon reflection that the  
12 use of several individual permutations instead of a single permutations provides a generic  
13 mechanism to defeat higher-order side-channel attacks and therefore this invention also  
14 provides a way to resist these more powerful attacks.

15 Thus the present invention provides a method including the steps of: providing a data processing  
16 operation involving at least one known lookup table, wherein each particular table from said at  
17 least one known lookup table has a particular lookup table size and a particular lookup table  
18 index size; creating at least one randomized table in which entries and/or indices are statistically  
19 independent of entries and/or indices of any table from said at least one known lookup table,  
20 each individual table from said at least one randomized table has a randomized table size,  
21 wherein a first sum of sizes of all said randomized tables is smaller than a second sum of sizes of  
22 all known lookup tables, and/or the maximum index size of said randomized tables is less than  
23 the maximum index size of the known lookup tables.

24 In some embodiments of the method, the method also includes performing said data processing  
25 operation employing said first randomized table; and/or the step of providing includes obtaining  
26 said data processing operation; and/or the step of creating said at least one randomized table  
27 includes the step of applying a Table Split operation to at least one of said known lookup tables  
28 resulting in split lookup tables; and/or the step of creating said at least one randomized table

1 includes the step of applying a Table Masking operation to at least one of said known lookup  
2 tables and/or split lookup tables resulting in masked tables; and/or the step of creating said at  
3 least one randomized table includes the step of applying a Table Aggregate operation to at least  
4 one of said masked tables.

5 It is noted that the step of applying a Table Split operation can use a variety of Table Splitting  
6 methods. For example, in an advantageous embodiment the step of applying a Table Split  
7 operation is performed by employing a Two-way Byte Table Splitting Method. Similarly, the  
8 step of applying a Table Masking operation can use a variety of table masking methods. For  
9 example, in an advantageous embodiment the step of applying a Table Mask operation is  
10 performed by employing an Input-Output Permutation Masking Method.

11 Similarly, the step of applying a Table Aggregate operation can use a variety of table  
12 aggregating methods. For example, in an advantageous embodiment the step of applying a Table  
13 Aggregate operation is performed by employing an Entry-wise Algebraic Aggregate Method. The  
14 known lookup table could be a table from any information security application or technique. For  
15 example the table could be from the COMP128 cryptographic algorithm or the Data Encryption  
16 Standard (DES) etc. For information security applications requiring resistance to side channel  
17 attacks, the method known as General Countermeasure Against Side-channel Attacks is usually  
18 employed as described earlier. Thus in some embodiments of this method, the lookup table is a  
19 table from an application of General Countermeasure Against Side Channel Attacks.

20 In some embodiments of the method, the number of elements in said at least one known lookup  
21 table is given by a power of two. As described earlier, those skilled in the art will easily  
22 recognize that having the number of elements in said at least one known lookup table be given by  
23 a power of two is particularly advantageous, since that provides the best efficiencies in the  
24 application of this invention. However, the methods described in the present invention are not  
25 limited to the case where the number of elements is a power of two, for example in one  
26 embodiment the number of elements in the lookup table is 200.

1 In some embodiments of the method, the said at least one randomized table is employed in a  
2 cryptographic process and the said at least one randomized table is used for securely handling  
3 information in said cryptographic process. In some of these embodiments, prior to performing  
4 said cryptographic process the information is transformed by applying a secret-sharing  
5 operation to the elements of the information where each element of the information is related to  
6 multiple elements of the transformed information, then the cryptographic process is performed on  
7 the transformed information involving the use of said at least one randomized table and then the  
8 transformed and cryptographically processed information is retransformed back by applying an  
9 inverse secret-sharing operation to yield the cryptographically processed information.

10 In some embodiments of the method the indices to at least one masked table of said plurality of  
11 masked tables are masked by a single permutation and data values in the masked table are  
12 masked by a single permutation and/or data processing operation is employed as a  
13 countermeasure against at least one first-order side-channel attack. In some embodiments, at  
14 least one higher-order side-channel attack is defeated by having the step of applying Table Mask  
15 operation include employing permutations for index and/or data values formed by composing  
16 several individual permutations

17 Thus the present invention also provides a method including the steps of: providing a lookup  
18 table for a data processing operation; performing a table split operation upon said lookup table in  
19 forming a collection of split tables; performing a table mask operation upon said collection of  
20 split tables and/or upon other lookup tables in forming a plurality of masked tables; performing a  
21 table aggregate operation on at least two of said plurality of masked tables in forming at least one  
22 aggregate table; and performing said data processing operation on a combination of split, masked  
23 aggregate and lookup tables.

24 Thus the present invention also provides a method including the steps of: providing a data  
25 processing operation involving at least one known lookup table, each particular table from said at  
26 least one known lookup table having a particular lookup table size and a particular lookup table  
27 index size; declaring any lookup table from said at least one known lookup table to be splittable:

1 if the table lookup size of said any lookup table is larger than an amount of RAM available, or if  
2 the table index size of said any lookup table is larger than available addressing capability;  
3 performing a table split operation upon said any lookup table declared splittable in the step of  
4 declaring and forming a collection of split tables; performing a table mask operation upon said  
5 collection of split tables and/or other of said known lookup tables forming a plurality of masked  
6 tables; performing said data processing operation on a combination of split, masked table,  
7 aggregate and lookup tables.

8 In some embodiments, of the method, the method further includes: performing at least one table  
9 aggregate operation on at least two of said plurality of masked tables forming at least one  
10 aggregate table; and/or the step of performing said data processing operation includes performing  
11 a table aggregate operation whenever a total size of all masked tables exceeds an amount of  
12 RAM available; and/or the step of providing includes obtaining the data processing operation.  
13 The step of performing Table Split is accomplished in various embodiments using a variety of  
14 table splitting methods.

15 In an advantageous embodiment the step of performing a Table Split operation employs the  
16 Output Divisor Table Splitting Method. Similarly, the step of performing Table Mask is  
17 accomplished in various embodiments using a variety of table masking methods. In an  
18 advantageous embodiment the step of performing a Table Mask operation employs the  
19 Input-Output XOR permutation Masking Method. Similarly, the step of performing Table  
20 Aggregate is accomplished in various embodiments using a variety of table aggregating methods.  
21 In an advantageous embodiment the step of performing a Table Aggregate operation employs the  
22 Byte-wise XOR Aggregate Method. In embodiments of the method, the step of performing said  
23 data processing operation involves any combination of aggregate, split, masked and known  
24 lookup tables. Thus, particular needs of an application may use aggregate and known tables and  
25 others may use some other combination. In general, many applications will use at least one of the  
26 masked and/or aggregate tables, and at least one of the known and/or split tables. In some of  
27 these embodiments only the split and masked tables are involved in this step, that is, there is no  
28 aggregate table. For example, this case occurs in an embodiment where there is enough

1 available RAM but the index of at least one known lookup table is large. In other embodiments  
2 only the aggregate tables and split tables are involved in this step, that is, the masked tables that  
3 were created have been aggregated into aggregated table. For example, this case occurs in an  
4 embodiment where there is very little available RAM and it is not feasible to keep an  
5 unaggregated masked table in RAM. In other embodiments all four of these tables are used.

6 Thus the present invention also provides a method including the steps of: providing a data  
7 processing operation involving a first lookup table, said lookup table having a first lookup table  
8 size and a first lookup table index size; creating a first randomized table in which entries; and/or  
9 indices are statistically independent of entries; and/or indices of said first lookup table, said first  
10 randomized table having a randomized table size being smaller than said first lookup table size;  
11 and/or a randomized table index size smaller than said first lookup table index size. In some  
12 embodiments of the method, the method further includes performing said data processing  
13 operation employing said first randomized table. In some embodiments of the method, there are  
14 multiple tables that need to be looked up thus in those embodiments the first lookup table is a  
15 first collection of tables. Also in some embodiments multiple randomized tables are created and  
16 thus the first randomized table is a first collection of randomized tables.

17 Thus the present invention also provides a method including the steps of: providing a data  
18 processing operation involving a first lookup table, said lookup table having a first lookup table  
19 size; creating a randomized table in which entries or indices are statistically independent of  
20 entries or indices of said first lookup table, said randomized table having a randomized table  
21 size being smaller than said first lookup table size. In some embodiments, the method further  
22 includes performing said data processing operation employing said randomized table.

23 Thus the present invention also provides a method including the steps of: providing a data  
24 processing operation involving a first lookup table in a cryptographic process, said lookup table  
25 having a first lookup table size; creating a randomized table in which entries or indices are  
26 statistically independent of entries or indices of said first lookup table, said randomized table  
27 having a randomized table size being smaller than said first lookup table size; employing said

1 randomized table for securely handling information in said cryptographic process; prior to  
2 performing the cryptographic process, transforming the information by applying a secret-sharing  
3 operation to the elements of the information where each element of the information is related to  
4 multiple elements of the transformed information; performing the cryptographic process on the  
5 transformed information involving the use of said randomized table; and retransforming the  
6 transformed and cryptographically processed information by applying an inverse secret-sharing  
7 operation to the transformed and cryptographically processed information.

8 In some embodiments of the method, the method also includes performing said data processing  
9 operation employing said randomized table. In some embodiments of the method, the  
10 cryptographic process is performed in a cryptographic information processing system or device.  
11 In some embodiments, any of the methods described herein is implemented as a module within a  
12 chip card.

13 The present invention is also realized as an apparatus in some embodiments. Figure 15 shows a  
14 generic diagram of one type of apparatus for realizing this invention. There are two main  
15 modules, the randomizer module (1500) and the processing module (1501). The randomizer  
16 module is responsible for creating random tables from a set of known tables. These known tables  
17 are either provided to the randomizer module or are generated by the randomizer by means of an  
18 optional module to create known tables (1501). The random tables have the property that their  
19 data values and indices are statistically independent of the data values and indices of the known  
20 tables. In some embodiments, the randomizer module contains a Splitting module to perform the  
21 Table Split operation (1502). In some embodiments, the randomizer module contains a Masking  
22 module to perform the Table Mask operation (1503). In some embodiments, the randomizer  
23 module contains an Aggregating module to perform the Table Aggregate operation (1504). A  
24 splitting module if present contains one or more modules for specific methods of performing the  
25 Table Split operation. For example it could contain a Unequal Table Splitter Module to perform  
26 the Unequal Table Splitting Method (1508); and/or it could contain other Table splitting method  
27 module or modules (1505). A masking module if present contains one or more modules for  
28 specific methods of performing the Table Mask operation. For example it could contain a

1 Input-Output XOR Permutation Masking Module (1509) to perform the Unequal Table Splitting  
2 Method; and/or it could contain other modules for some other Table Masking method (1506). An  
3 aggregating module if present contains one or more modules for specific methods of performing  
4 the Table Aggregate operation. For example it could contain a Byte-wise XOR Aggregating  
5 Module (1510) to perform the Byte-wise XOR Aggregating Method; and/or it could contain  
6 other modules for some other Table Aggregating method (1507).

7 Thus, the present invention is also realized as an apparatus. In some embodiments, the apparatus  
8 includes: a randomizer module to create at least one randomized table in which entries and/or  
9 indices are statistically independent of entries, and/or indices of any table from a provided set of  
10 known lookup tables, each individual table from said at least one randomized table having a  
11 randomized table size, wherein a first sum of sizes of all said randomized tables is smaller than a  
12 second sum of sizes of all said at least one known lookup tables, and/or the maximum index size  
13 of said randomized tables is less than the maximum index size of the known lookup tables; and a  
14 processing module to perform said data processing operation employing said first randomized  
15 table.

16 In some embodiments of the apparatus the randomizer module forms said provided set of known  
17 lookup tables; and/or the randomizer module includes a splitting module to perform a Table Split  
18 operation upon at least a subset of said set of known lookup tables resulting in split lookup  
19 tables; and/or the randomizer module includes a masking module to perform a Table Masking  
20 operation upon at least a subset of said set of known lookup tables; and/or split lookup tables  
21 forming a set of masked tables; and/or the randomizing module includes an aggregating module  
22 to perform a Table Aggregate operation to at least one masked table.

23 In some embodiments of the apparatus, the splitting module within the randomizer module  
24 includes an Unequal Table Splitter Module which applies the Unequal Table Split Method for  
25 performing a Table Split Operation. In some embodiments of the apparatus, the masking module  
26 within the randomizer module includes an Input-Output XOR Permutation Masking module  
27 which applies the Input-Output XOR Permutation Masking Method for performing a Table  
28 Mask Operation. In some embodiments of the apparatus, the aggregating module within the

1 randomizer module includes an Byte-wise XOR Aggregating Module which applies the  
2 Byte-wise XOR Aggregating Method for performing a Table Aggregate Operation.

3 Thus the present invention is also realized as an apparatus including: a splitting module to  
4 perform a table split operation upon a provided set of lookup tables, forming a collection of split  
5 tables; a masking module to perform a table mask operation upon said collection of split tables;  
6 and/or other lookup tables forming a plurality of masked tables; an aggregating module to  
7 perform a table aggregate operation on a subset of said plurality of masked tables; and a  
8 processing module to perform said data processing operation.

9 The present invention can be realized in hardware, software, or a combination of hardware and  
10 software. A visualization tool according to the present invention can be realized in a centralized  
11 fashion in one computer system, or in a distributed fashion where different elements are spread  
12 across several interconnected computer systems. Any kind of computer system - or other  
13 apparatus adapted for carrying out the methods and/or functions described herein - is suitable. A  
14 typical combination of hardware and software could be a general purpose computer system with  
15 a computer program that, when being loaded and executed, controls the computer system such  
16 that it carries out the methods described herein. The present invention can also be embedded in a  
17 computer program product, which comprises all the features enabling the implementation of the  
18 methods described herein, and which - when loaded in a computer system - is able to carry out  
19 these methods.

20 Computer program means or computer program in the present context include any expression, in  
21 any language, code or notation, of a set of instructions intended to cause a system having an  
22 information processing capability to perform a particular function either directly or after either  
23 or both of the following conversion to another language, code or notation, and/or reproduction in  
24 a different material form.

25 Thus the invention includes an article of manufacture which comprises a computer usable  
26 medium having computer readable program code means embodied therein for causing a function

1 described above. The computer readable program code means in the article of manufacture  
2 comprises computer readable program code means for causing a computer to effect the steps of a  
3 method of this invention.

4 Similarly, the present invention may be implemented as a computer program product comprising  
5 a computer usable medium having computer readable program code means embodied therein for  
6 causing a function described above. The computer readable program code means in the  
7 computer program product comprising computer readable program code means for causing a  
8 computer to effect one or more functions of this invention. Furthermore, the present invention  
9 may be implemented as a program storage device readable by machine, tangibly embodying a  
10 program of instructions executable by the machine to perform method steps for causing one or  
11 more functions of this invention.

12 It is noted that the foregoing has outlined some of the more pertinent objects and embodiments of  
13 the present invention. This invention may be used for many applications. Thus, although the  
14 description is made for particular arrangements and methods, the intent and concept of the  
15 invention is suitable and applicable to other arrangements and applications. For example,  
16 although the description indicates use of the present invention for known lookup tables it is most  
17 particularly applicable to fixed lookup tables. It will be clear to those skilled in the art that  
18 modifications to the disclosed embodiments can be effected without departing from the spirit and  
19 scope of the invention. The described embodiments ought to be construed to be merely  
20 illustrative of some of the more prominent features and applications of the invention. Other  
21 beneficial results can be realized by applying the disclosed invention in a different manner or  
22 modifying the invention in ways known to those familiar with the art.